



## Modeling and Analysis of Triple Play Services in Multimedia Internet

Natalia M. Markovich ICS, Russian Academy of Sciences, Moscow

Tien Van Do Budapest University of Technology and Economics, Budapest

Udo R. Krieger Otto-Friedrich Universität, Bamberg

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# Outline

- Part I: Service Architecture of Multimedia Internet
  - Infrastructure of a multimedia Internet
  - Protocol structures of multimedia services
  - Resource management and multi-processing strategies
- Part II: Modeling and Analysis of an Apache Web Server
  - A queueing network describing a dynamic pool of service processes
  - Workload modeling and performance analysis at the page layer
- Part III: Service Analysis of a Media Server
  - Performance modeling at the session level by a multi-class loss system
- Part IV: Analysis of Packet-Switched Multimedia Streams
  - Characterization of multimedia packet streams by measured data
  - Statistical modeling of Qos indicators by a bufferless fluid approach
  - Capacity requirements of peer-to-peer and VBR packet traffic
- Part V: Conclusions and Open Issues









## Network Structure and Layering in IPTV Architectures



#### **Distribution Layer**

- dissemination of content
- provided by an overlay infrastructure

#### Transport Layer

- physical transport infrastructure with optical signal transport in the core and close to the homes
- on top of a packet-switched network
- use of RTP/RTSP combined with QoS supported TCP/UDP/IP stack
- SIP signaling applied























# Virtualization of Server Processing

• virtualization of task processing, resource assignment and management in current operating systems

• a virtualization layer (VMM/VM) separates physical hardware and resource demands of application processing

- integration of different operating systems (guest OS)
  - running on one physical system (host





#### Example: VMware Infrastructure Consolidated HA VMotion DRS lackus. VirtualCenter Management Server **Virtual Machines** Virtual SMP ESX Server Enterprise servers Enterprise network **Enterprise Storage**

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# Liu's Workload Modeling at the Page Layer



### Level-Dependent Matrix-Geometric Model

- System model Z(t) = (I(t), J(t))
  - CTMC on finite state space {1,.., M×N} x {0,..,L}
- level J(t)
  - number j of TCP sessions served or waiting in the listen queue
- phase  $I(t) = F(I_1(t), I_2(t))$  determined by
  - modulator variable  $I_1(t) = i \in \{1, ..., M\}$  of a *Markov-modulated batch arrival* stream with M states (compound Poisson process)
    - having a generalized exponential (GE) interarrival time  $\tau$  with distribution in phase i:  $\Pr(0 < \tau_i < t) = (1 - \theta_i)(1 - e^{-\sigma_i t})$
    - random batches S of size s with distribution  $(1 \theta_i)\theta_i^{s-1}$
  - random number  $1 \le I_2(t) = h \le N$  of available HTTP service processes
    - governed by exponentially distributed creation and killing times of pooled servers with rates  $\eta$  and  $\epsilon$

# State-Dependent Service Time Modeling



- service time as result of complex interaction
  - of the contention at physical resources: CPUs, disk operations
  - TCP flow control and segment transfer in the Internet
- application of Menasce's QNW model
  - aproximation of the state-dependent service rate  $\mu(p,k)$  by the throughput  $T_p(k)$ of a closed QNW
  - given k requests served by p active processes in the system
  - $T_p(k) = T_p(p), \quad k \ge p$
- applied alternative:
  - identification by measurements
- compromise: accuracy vs. complexity



Performance Measures

 • mean number of idle service processes

 
$$E(Idle) = \sum_{i=1}^{NM} \sum_{j=0}^{L} p_{i,j} \cdot \max(f_2(i) - j, 0)$$

 • probability  $p_W$  that a new request is waiting for an idle child process

  $p_W = \sum_{i=1}^{NM} \sum_{j=0}^{L} \sum_{s=\max(f_2(i)-j,0)+1}^{\infty} p_{i,j} \cdot (1 - \theta_{f_1(i)}) \theta_{f_1(i)}^{s-1} \cdot \frac{\min((s - \max(f_2(i) - j, 0), L - j)\sigma_{f_1(i)})}{\overline{\sigma}}$ 

 • with mean arrival rate  $\overline{\sigma} = \sum_{l=1}^{M} \frac{\sigma_l}{(1 - \theta_l)} r_l$ 

 • and steady state vector r of the modulator  $l_1$ :

  $\mathbf{r} \cdot Q_X = 0$  ;  $\mathbf{r} \cdot e_M = 1$ .

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### Validation of the Approach by Measurements

		Parameters		Ν	leasurement	t Study		Analytic M	odel
σ	θ	$\eta$	$\epsilon$	E(Idle)	Var(Idle)	Waiting Prob.	E(Idle)	Var(Idle)	Waiting Prob.
5	0.4	0.003960	0.001500	9.92740	0.4323	0.000087	9.933774	0.333595	0.0001343
5	0.5	0.007042	0.003130	9.89174	0.6153	0.003466	9.906068	0.437426	0.0012225
5	0.6	0.011198	0.007337	9.83198	0.8833	0.015859	9.858125	0.602280	0.0075010
5	0.7	0.020465	0.016675	9.70886	1.3312	0.056009	9.762665	0.895090	0.0352133
5	0.8	0.062304	0.058661	9.47287	2.0765	0.175968	9.545315	1.460498	0.1346032
5	0.9	0.230746	0.227524	9.23774	3.8538	0.385522	8.876794	2.732862	0.3576490
10	0.4	0.006120	0.001749	9.87653	0.5695	0.000028	9.865037	0.477537	0.0001713
10	0.5	0.007774	0.003455	9.82228	0.7829	0.002989	9.812958	0.618592	0.0015107
10	0.6	0.016354	0.012161	9.72373	1.1271	0.015115	9.716133	0.852531	0.0092000
10	0.7	0.040675	0.036607	9.54612	1.6814	0.056359	9.525983	1.265490	0.0433613
10	0.8	0.095757	0.091942	9.15435	2.5931	0.178238	9.098354	2.055569	0.1681403
10	0.9	0.330487	0.327367	9.00565	4 5981	0.360757	7 918966	3 700704	0.4302934
20	0.4	0.007869	0.002951	9.82219	0.6871	0.000782	9.733936	0.671095	0.0002637
20	0.5	0.012012	0.007207	9.74126	0.9354	0.003211	9.628082	0.872976	0.0022319

• model validation in a test bed

- generation of HTTP traffic by Apache benchmark tool *ab*
- only HTTP 1.0 used and *renewal model* applied
- model parameters: hmin = 5, hmax=10, N=30, L = 40

•relative accuracy of the model subject to the measurements:

• mean number of idle processes: 3%; variance 20 % deviation; abserr(wait prob) <8%





### **Object-Dependent Arrival Streams**

- popularity-dependent request patterns for streamed objects
  - modelled by M object classes i
  - requests determined by Zipf-Mandelbrot law

$$f_i(\alpha, k) = C \cdot \frac{1}{(i+k)^{\alpha}}, \quad i \in \mathbb{N}, k \in \mathbb{N}, \alpha \in \mathbb{R}^+$$

$$C^{-1} = \sum_{i} \frac{1}{(i+k)^{\alpha}}$$

simplest heavy-tailed case used here: Zipf law

$$f_i = f_i(\alpha, 0) = C \cdot \frac{1}{i^{\alpha}}$$

- request streams to objects
  - modelled by M Poisson streams of rate λ<sub>i</sub>
  - rate estimation using non-homogeneous Poisson processes







## **Bandwidth Modeling**

- Bandwidth modeling
  - apply basic bandwidth units (BBU) of fixed sized b<sub>0</sub>
    - e.g. b<sub>0</sub>=64 kbps or 32 kbps
  - determines K traffic classes
- Bandwidth requirement
  - depends on used codec and spatial resolution

SQCIF	(128 x 96)
QCIF	(176 x 144)
CIF	(352 x 288)
4CIF	(704 x 576)
16CIF	(1408 x 1152)

- can use a *peak-bandwidth* description
  - approach applied here
- or sustainable or equivalent bandwidth model (R. Guerin and others)
  - often too complex
  - requires burst level modeling, e.g. by on-off sources, at packet level
- traffic classes of objects

 $TC_i = \{j \in \{1, 2, \dots, M\} | b(O_j) = c_i\}$ 

## Modeling Service Durations

- three main object-dependent components for each class i
  - playback time D<sub>i</sub>
    - determined by length and rate of the video stream
    - deterministic length of mean 1/d<sub>i</sub>
    - · modelled by an exponential distribution
  - inspection time l<sub>i</sub>
    - · determined by object type and user behavior
    - mixture of exponential and uniform distribution
    - modelled by an exponential distribution with mean  $1/\chi_i$
  - selection ratio  $\beta_i$  for a full playback of the video stream



### Modeling Service Durations

Service time distribution function

$$F_{i}(x) = \mathbb{P}\{S_{i} \leq x\} = \beta_{i} \mathbb{P}\{D_{i} \leq x\} + (1 - \beta_{i}) \mathbb{P}\{\min(I_{i}, D_{i}) \leq x\}$$
$$= \beta_{i} \mathbb{P}\{D_{i} \leq x\} + (1 - \beta_{i})[1 - (1 - \mathbb{P}\{I_{i} \leq x\})(1 - \mathbb{P}\{D_{i} \leq x\})]$$

• Mean service time

$$\begin{split} \mathbb{E}(S_i) &= 1/\mu_i = \beta_i \frac{1}{d_i} + (1 - \beta_i) \frac{1}{d_i + \chi_i} \\ &= \frac{\beta_i \chi_i + d_i}{d_i (d_i + \chi_i)} \\ &= \frac{\mathbb{E}(S_i)(\beta_i \mathbb{E}(S_i) + \mathbb{E}(I_i))}{\mathbb{E}(I_i) + \mathbb{E}(S_i)} \end{split}$$

• Mean service time of an aggregated traffic stream

$$\mathbb{E}(T_i) = 1/\tau_i = \sum_{j \in TC_i} \frac{\lambda_j}{\xi_i} \frac{\mathbb{E}(D_j)}{\mathbb{E}(D_j) + \mathbb{E}(I_j)} [\beta_j \mathbb{E}(D_j) + \mathbb{E}(I_j)]$$



#### Product-Form Steady-State Distribution

•State space

$$\Sigma = \{n = (n_1, \dots, n_K) \in \mathbb{N}_0^K | 0 \le n_i \le \lfloor C/b_i \rfloor, i \in \{1, \dots, K\}, b^t n \le C\}$$
  

$$\Sigma(j) = \{n \in \Sigma | b^t n = j\}$$
  

$$\Sigma_k = \bigcup_{j=0}^C \Sigma(j - b^t e_k) = \{n \in \Sigma | b^t n \le C - b_k\}$$
  

$$\Sigma_0 = \bigcup_{i=0}^C \Sigma(j) = \{n \in \Sigma | b^t n \le C\}$$

•Steady-state distribution of class-related Markov vector process  $X(t) = (X_i(t))$ 

$$\begin{aligned} \pi(n) &= \frac{1}{G} \cdot \prod_{i=1}^{K} \frac{\rho_{i}^{n_{i}}}{n_{i}!}, \quad n \in \Sigma, \quad G = \sum_{n \in \Sigma} \prod_{i=1}^{K} \frac{\rho_{i}^{n_{i}}}{n_{i}!} \quad \rho_{i} = \rho_{i}(\alpha) = \lambda_{i}/\mu_{i} = \lambda p_{i}(\alpha)/\mu_{i} \end{aligned}$$

$$\begin{aligned} q(j) &= \sum_{n \in \Sigma(j)} \pi(n), \quad R_{k}(j) = \sum_{n \in \Sigma(j)} n_{k} \pi(n) \quad q(j) = \frac{1}{j} \sum_{i=1}^{K} b_{i}\rho_{i} q(j-b_{i}), \quad j = 0, 1, \dots, C \end{aligned}$$

$$\begin{aligned} G(C) &= \sum_{n \in \Sigma_{0}} \prod_{i=1}^{K} \frac{\rho_{i}^{n_{i}}}{n_{i}!}, \quad G(C-b_{k}) = \sum_{n \in \Sigma_{k}} \prod_{i=1}^{K} \frac{\rho_{i}^{n_{i}}}{n_{i}!} \end{aligned}$$

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#### **Performance Characteristics**

Utilization

$$Y = b^t \cdot X,$$

$$U = \mathbb{IE}(Y) = \sum_{j=0}^{C} j \mathbb{IP}\{b^{t}X = j\} = \sum_{j=1}^{C} jq(j)$$

Blocking of service class i

$$B_{i} = 1 - \mathbb{P}\{b^{t}X \le C - b^{t}e_{i}\} = 1 - \frac{G(C - b_{i})}{G(C)}$$

Throughput of class i

$$T_i = \lambda_i \cdot (1 - B_i)$$

Arrival-Sensitivity on the Tail-Index of the Popularity Distribution

• given Poisson r.v.  $Y_j \sim \operatorname{Pois}(\rho_j(\alpha))$ 

$$\mathbb{P}\{Y_j = n\} = e^{-\rho_j(\alpha)} \ \frac{\rho_j(\alpha)^n}{n!}$$

exhibits monotonicity in log-likelihood ordering



- monotone increasing in  $\lambda_j$  decreasing in  $\mu_j$
- behavior in  $\boldsymbol{\alpha}$  depends on class j
- occupancy X<sub>i</sub> and thoughput behavior inherited

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#### Case Study and its Parameter Settings

Illustration of the Markovian modeling approach

p(1.2, 3)	—	$(0.587, 0.256, 0.157)^t$
p(1.5, 3)		$(0.647, 0.229, 0.124)^t$
p(2,3)	_	$(0.735, 0.184, 0.082)^t$

$$\mu_1 = 1.5, \mu_2 = 1, \mu_3 = 0.833,$$
  
 $b = (1, 2, 3)^t.$ 

C	$B_1$	$B_2$	$B_3$	GB	$TH_1$	$TH_2$	$TH_3$	U	U/C
400	0.034	0.067	0.099	0.053	5.672	2.385	1.416	373.497	0.934
300	0.044	0.087	0.128	0.068	5.611	2.334	1.37	279.887	0.933
200	0.064	0.124	0.18	0.098	5.497	2.239	1.288	186.29	0.931
140	0.087	0.166	0.24	0.131	5.363	2.131	1.195	130.146	0.93
120	0.098	0.188	0.269	0.148	5.294	2.076	1.149	111.437	0.929
100	0.114	0.216	0.307	0.17	5.203	2.005	1.09	92.733	0.927
80	0.135	0.254	0.357	0.2	5.077	1.908	1.011	74.037	0.925
60	0.167	0.308	0.427	0.244	4.89	1.768	0.901	55.353	0.923
40	0.22	0.394	0.532	0.314	4.581	1.548	0.735	36.696	0.917
20	0.328	0.554	0.708	0.446	3.946	1.139	0.458	18.103	0.905

Table 1: Study of a streaming media system with three service classes

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# Skype Traffic Measurements

•prototypical home environment with 2 wireless segments and ADSL attachments





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### Statistical Analysis After Data Partitioning

Requirements of a statistical analysis: stationarity and independence

- pure stationarity not a realistic assumption for real data sets of triple play streams
- independence achievable by partitioning of data into independent blocks of fixed or variable lengths  $L_j = \sum_{i=kj} k_j^{kj-1+Nj} X_i$ ,  $j = 1, ..., N_s$ 
  - e.g. by exceedances over the empirical 97% quantiles of the IATs {X<sub>i</sub>}
  - proof of independence by appropriate statistical Portmanteau tests (Runde, Lung-Box etc.)



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### Features of P2P and VBR Packet Traffic

- often long-range dependent time series of IATs {X<sub>i</sub>} with heavy-tailed marginal distributions F(x) = 1 - x <sup>-α</sup> I(x)
  - determined by Hill's estimate of the extreme value index  $\gamma = 1/\alpha$  on the order statistics  $X_{(i)}$  $\widehat{\gamma}^{H}(n,k) = \frac{1}{k} \sum_{i=1}^{k} \ln X_{(n-i+1)} - \ln X_{(n-k)}$

• extremal index  $\theta$  of maxima  $M_n = \max X_i$  of IATs in blocks

$$\mathbb{P}\{M_n \le u\} \approx \mathbb{P}^{\theta}\{\widetilde{M}_n \le u\} = F^{n\theta}(u)$$

Features	Skype Data			1		
	IAT	$\mathbf{PL}$	Block duration	IAT	IAT Block maxima	
Independence	8 <b>1</b> —35	<u></u>	+	-	+	M
LRD	+	+	( <del></del>	+	_	ind
Self-similarity	+	+	+	+	+	lea
Heavy-tailed	+	<u>(2.0</u> )	-	<u></u>	+	lieli
with finite variance Heavy-tailed with infinite variance	-	-	+	+	<del></del>	E3
Light-tailed	3. <del>-</del> 32	+	-			

Example: Sopcast over a WLAN



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# Delivery Time Variation in a Bufferless Fluid Model



- determined for completely transferred packets by  $y_i = \tau_i - \tau_{i-1} = t_i + d_i - (t_{i-1} + d_{i-1}) = \Delta t_i + \Delta d_i$ IATs at departure  $\Delta t_i$  with mean EX and delay jitter  $\Delta d_i$
- •mean delivery time variation in case of data loss  $d = (1 + 1/\theta) EX$ 
  - with mean cluster size  $1/\theta$
- derived from extremal index  $\theta \in [0, 1]$ 
  - as indicator of changes in limiting df of  $\max_i R_i$

- working with representatives of QoS indicators in data blocks (*EVT block method*)
  - such as extreme rate values max R<sub>i</sub>
- using instantaneous traffic rates  $R_i = Y_i/X_i$ overshooting a capacity threshold u









## Conclusions

- single-tier Web server architecture
  - study of Apache's non-threaded multi-processing module Prefork
    - Markovian modeling by a queueing network with batch Markovian arrival process and a dynamic number of servers
  - potential extensions
    - hybrid thread/process UNIX module MPM Worker
    - · extension of the QNW model to heavy-tailed service times
- single-tier streaming media server architecture
  - Markovian modeling by a Erlang loss model
    - with popularity-dependent Poissonian batch Markovian arrival process
      - traffic classes determined by CBR bandwidth requirements
      - service times including object-dependent inspection behavior
    - closed-form analysis of resulting  $\Sigma M^{X}/M/C/C$  loss model
  - potential extensions
    - QNW model with heavy-tailed service times
    - optimized access control and bandwidth assignment for a server farm model
- nonparametric statistical traffic characterization and Qos/QoE analysis of VBR or P2P packet traffic









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